

IB Math AA HL Chapter 2 Quadratic Equations, Functions and Inequalities Notes

Remember with quadratics the graph is a parabola. Parabolas are symmetric and the axis of symmetry is down the middle of the graph. A parabola can cross the x-axis once, twice or not at all. The point(s) where the graph crosses the x-axis are called the zeros of the function or the roots of the equation.

$$y = (x - a)^2 \text{ horizontal translation}$$

$$y = x^2 + a \text{ vertical translation}$$

$$y = ax^2 \text{ vertical reflection and vertical dilation}$$

Different forms of quadratic functions/equations

Standard form $y = ax^2 + bx + c$

Factored form $y = a(x - r_1)(x - r_2)$

Intercept form $y = (ax + b)(cx + d)$ intercepts $\left(\frac{-b}{a}\right)$ or $\left(\frac{-d}{c}\right)$

Turning point form (Vertex form) $y = a(x - p)^2 + q$ turning point/vertex (p, q)

Quadratic formula: If $y = ax^2 + bx + c$, then $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$.

Discriminant $b^2 - 4ac$ Use the discriminant to determine the nature of the roots.

if $b^2 - 4ac > 0$ 2 real roots

if $b^2 - 4ac = 0$ 1 real root

if $b^2 - 4ac < 0$ 2 complex roots

Sum and product of roots for quadratic equations: Sum: $-\frac{b}{a}$ Product: $\frac{c}{a}$

Completing the square: $ax^2 + bx + c$

You Try: Complete the square.

$$4x^2 + 40x + 125$$

1. Take out a, leaving the constant alone: $a\left(x^2 + \frac{b}{a}x\right) + c$

2. Complete the square and factor: $a\left[\left(x + \frac{b}{2a}\right)^2 - \left(\frac{b}{2a}\right)^2\right] + c$

3. Multiply out the outer bracket: $a\left(x + \frac{b}{2a}\right)^2 - \frac{b^2}{4a} + c$

4. Tidy up the constants: $a\left(x + \frac{b}{2a}\right)^2 - \left(\frac{b^2 - 4ac}{4a}\right)$

Graphing inequalities (linear or quadratic):

1. Graph as if the inequality was an equal sign.

2. Shade the solution area. (pick a point, use end behavior or read the inequality sign)